



# GEOMETRICAL FRAMEWORK OF QUANTIZATION PROBLEM

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**Abstract.** The basic elements of the geometric approach to a consistent quantization formalism are summarized, with reference to the methods of the old quantum mechanics and the induced representations theory of Lie groups. A possible relationship between quantization and phase-space discretization is briefly discussed.

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