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*Forcing with ideals generated by closed sets*

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**Abstract:** Consider the poset  $P_I = \text{Borel}(\mathbb{R}) \setminus I$  where  $I$  is an arbitrary  $\sigma$ -ideal  $\sigma$ -generated by a projective collection of closed sets. Then the  $P_I$  extension is given by a single real  $r$  of an almost minimal degree: every real  $s \in V[r]$  is Cohen-generic over  $V$  or  $V[s] = V[r]$ .

**Keywords:** forcing, descriptive set theory, large cardinals

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