

HYPERKÄHLER METRICS FROM PROJECTIVE SUPERSPACE

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ABSTRACT. This is a brief review of how sigma models in Projective Superspace have become important tools for constructing new hyperkähler metrics.

1. INTRODUCTION

The close relation between supersymmetric sigma models and complex geometry was first observed almost thirty years ago in [27]. For $\mathcal{N} = 2$ models in four dimensions the target space geometry was subsequently shown to be hyperkähler in [1]. This fact was extensively exploited in a $\mathcal{N} = 1$ superspace formulation of these models in [22], where two new constructions were presented; the Legendre transform construction and the hyperkähler quotient construction. The latter reduction was given a mathematical formulation in [12] where we also elaborated on a manifest $\mathcal{N} = 2$ formulation, originally introduced in [5].

A $\mathcal{N} = 2$ superspace formulation of the $\mathcal{N} = 2$ sigma model is obviously desirable, since it will automatically lead to hyperkähler geometry on the target space. The $\mathcal{N} = 2$ Projective Superspace which makes this possible grew out of the development mentioned in the last sentence in the paragraph above. Over the years it has been developed and refined in, e.g., [15]-[9]. In this article we report on some of that development along with some very recent applications.

2. SIGMA MODELS

A supersymmetric non-linear sigma model is given by maps from a (super) manifold $\Sigma^{(d,\mathcal{N})}$ to a target space \mathcal{T} :

$$(2.1) \quad \Phi: \Sigma^{(d,\mathcal{N})} \longmapsto \mathcal{T},$$

defined by giving an action involving an integral over $\Sigma^{(d,\mathcal{N})}$. For a two-dimensional model in $\mathcal{N} = (1, 1)$ superspace ($d = 2$, $\mathcal{N} = (1, 1)$) the action is

$$(2.2) \quad S = \int_{\Sigma} d^2\xi d^2\theta D_+ \Phi^\mu E_{\mu\nu}(\Phi) D_- \Phi^\nu,$$

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where ξ, θ are coordinates on Σ , the superspace covariant derivatives satisfy $D_{\pm}^2 = i\partial_{\pm}$, and $E_{\mu\nu} \equiv G_{\mu\nu} + B_{\mu\nu}$ is the sum of the metric and antisymmetric B -field. The field equations are

$$(2.3) \quad \nabla_+^{(+)} D_- \Phi^\mu = 0$$

which involves the pullback of the covariant derivative $\nabla^{(+)} \equiv \nabla + G^{-1}H$, the sum of the Levi-Civita connection and the torsion built from the field-strength of the B -field; $H = dB$. The rôle of the geometry of \mathcal{T} is becoming evident from the geometric objects introduced. The type of geometry depends on (d, \mathcal{N}) , i.e., on the bosonic dimension of Σ and on the number of supersymmetries. We illustrate with a couple of examples.

Example 1.

The model defined by the action (2.2) has $\mathcal{N} = (2, 2)$ supersymmetry provided that the target space carries a certain bi-hermitean geometry [5], or in its modern guise, Generalized Kähler Geometry [13] [11]. In this case, there is a manifest $\mathcal{N} = (2, 2)$ formulation

$$(2.4) \quad S = \int_M \mathbb{D}^2 \mathbb{D}^2 K(\mathbb{X}_L, \bar{\mathbb{X}}_L, \mathbb{X}_R, \bar{\mathbb{X}}_R, \phi, \bar{\phi}, \chi, \bar{\chi}),$$

where the Lagrangian K is a function of the chiral ϕ and twisted chiral fields χ as well as the semichiral fields [3], $\mathbb{X}_{L,R}$. These fields are defined as follows:

$$(2.5) \quad \begin{aligned} \bar{\mathbb{D}}_+ \mathbb{X}_L &= \mathbb{D}_+ \bar{\mathbb{X}}_L = 0, \\ \bar{\mathbb{D}}_- \mathbb{X}_R &= \mathbb{D}_- \bar{\mathbb{X}}_R = 0, \\ \bar{\mathbb{D}}_{\pm} \phi &= \mathbb{D}_{\pm} \bar{\phi} = 0 \\ \bar{\mathbb{D}}_+ \chi &= \mathbb{D}_- \chi = \mathbb{D}_+ \bar{\chi} = \bar{\mathbb{D}}_- \bar{\chi} = 0, \end{aligned}$$

where \mathbb{D} is the $\mathcal{N} = (2, 2)$ covariant derivative. All geometric quantities in this geometry have a local expression involving derivatives of the Generalized Kähler potential K [25]. These expressions, in particular those for the metric and B -field, are non-linear functions of $\partial\bar{\partial}K$, nonlinearities that can be explained by the fact that the geometry may be constructed by a quotient from a higher dimensional space [26].

Example 2.

Consider the previous example without a B -field. When the number of supersymmetries are further increased to $\mathcal{N} = (4, 4)$, the target space geometry is restricted to be hyperkähler. The Kähler potential is $K(\phi, \bar{\phi})$ and the additional supersymmetries are non-manifest, i.e., explicit transformations of the chiral and semichiral superfields. These transformations involve the additional two complex structures of the hyperkähler geometry, and the algebra of the extra supersymmetries typically only close on-shell, i.e., modulo field equations.

3. PROJECTIVE SUPERSPACE

In the second example above, the $\mathcal{N} = (2, 2)$ formulation of the $\mathcal{N} = (4, 4)$ models require explicit transformations on the $\mathcal{N} = (2, 2)$ superfields that close to the supersymmetry algebra on-shell. This non-manifest formulation makes the construction of new models difficult. Below follows a brief description of a superspace where all supersymmetries are manifest. This “projective superspace” [15]-[9] has been developed in parallel to harmonic superspace [4]. The relation between the two approaches is discussed in [17].

A hyperkähler space \mathcal{T} supports three globally defined integrable complex structures I, J, K obeying the quaternion algebra: $IJ = -JI = K$, plus cyclic permutations. Any linear combination of these, $aI + bJ + cK$ is again a complex structure on \mathcal{T} if $a^2 + b^2 + c^2 = 1$, i.e., if $\{a, b, c\}$ lies on a two-sphere $S^2 \simeq \mathbb{P}^1$. The Twistor space \mathcal{Z} of a hyperkähler space \mathcal{T} is the product of \mathcal{T} with this two-sphere $\mathcal{Z} = \mathcal{T} \times \mathbb{P}^1$. The two-sphere thus parametrizes the complex structures and we choose projective coordinates ζ to describe it (in a patch including the north pole). It is an interesting and remarkable fact that the very same S^2 arises in an extension of superspace to accomodate manifold $\mathcal{N} = (4, 4)$ models.

The algebra of $\mathcal{N} = (4, 4)$ superspace derivatives is

$$(3.6) \quad \begin{aligned} \{\mathbb{D}_{a\pm}, \bar{\mathbb{D}}_{\pm}^b\} &= \pm i \delta_a^b \partial_{\pm} & \{\mathbb{D}_{a\pm}, \mathbb{D}_{b\pm}\} &= 0, \\ \{\mathbb{D}_{a\pm}, \mathbb{D}_{b\mp}\} &= 0, & \{\mathbb{D}_{a\pm}, \bar{\mathbb{D}}_{\mp}^b\} &= 0. \end{aligned}$$

We may parameterize a \mathbb{P}^1 of maximal graded abelian subalgebras as (suppressing the spinor indices)

$$(3.7) \quad \nabla(\zeta) = \mathbb{D}_2 + \zeta \mathbb{D}_1, \quad \bar{\nabla}(\zeta) = \bar{\mathbb{D}}^1 - \zeta \bar{\mathbb{D}}^2,$$

where ζ is the coordinate introduced above, and the bar on ∇ denotes conjugation with respect to a real structure \mathfrak{R} defined as complex conjugation composed with the antipodal map on $\mathbb{P}^1 \simeq S^2$. The two new covariant derivatives in (3.7) anti-commute

$$(3.8) \quad \{\nabla, \bar{\nabla}\} = 0.$$

They may be used to introduce constraints on superfields similarly to how the $\mathcal{N} = (2, 2)$ derivatives are used to impose chirality constraints in (2.5). Superfields now live in an extended superspace with coordinates ξ, ζ, θ . The superfields Υ we shall be interested in satisfy the projective chirality constraint

$$(3.9) \quad \nabla \Upsilon = \bar{\nabla} \Upsilon = 0,$$

and are taken to have the following ζ -expansion:

$$(3.10) \quad \Upsilon = \sum_i \Upsilon_i \zeta^i.$$

We use the real structure acting on superfields, $\mathfrak{R}(\Upsilon) \equiv \bar{\Upsilon}$, to impose reality conditions on the superfields. An $\mathcal{O}(2n)$ multiplet is thus defined via

$$(3.11) \quad \Upsilon \equiv \eta_{(2n)} = (-)^n \zeta^{2n} \bar{\Upsilon}.$$

The expansion (6.26) is useful in displaying the $\mathcal{N} = (2, 2)$ content of the multiplets. Using the relation (3.7) to the $\mathcal{N} = (2, 2)$ derivatives in (3.9) we read off the following expansion for an $\mathcal{O}(4)$ multiplet (3.11):

$$(3.12) \quad \eta_{(4)} = \phi + \zeta \Sigma + \zeta^2 X - \zeta^3 \bar{\Sigma} + \zeta^4 \bar{\phi},$$

with the component $\mathcal{N} = (2, 2)$ fields being chiral ϕ , unconstrained X and complex linear Σ . A complex linear field satisfies

$$(3.13) \quad \bar{\mathbb{D}}^2 \Sigma = 0,$$

and is dual to a chiral superfield. A general projective chiral Υ has the expansion

$$(3.14) \quad \Upsilon = \phi + \zeta \Sigma + \sum_{i=2}^{\infty} X_i \zeta^i,$$

with all X_i 's unconstrained.

4. THE GENERALIZED LEGENDRE TRANSFORM

In this section we review one particular construction of hyperkähler metrics using projective superspace introduced in [23].

An $\mathcal{N} = (4, 4)$ invariant action may be written as

$$(4.15) \quad S = \int \mathbb{D}^2 \bar{\mathbb{D}}^2 F,$$

with

$$(4.16) \quad F \equiv \oint_C \frac{d\zeta}{2\pi i \zeta} f(\Upsilon, \bar{\Upsilon}; \zeta),$$

for some suitably defined contour C . Eliminating the auxiliary fields X_i by their equations of motion will yield an $\mathcal{N} = (2, 2)$ model defined on the tangent bundle $T(\mathcal{T})$ parametrized by (ϕ, Σ) . Dualizing the complex linear fields Σ to chiral fields $\tilde{\phi}$ the final result is a supersymmetric $\mathcal{N} = (2, 2)$ sigma model in terms of $(\phi, \tilde{\phi})$ which is guaranteed by construction to have $\mathcal{N} = (4, 4)$ supersymmetry, and thus to define a hyperkähler metric. In equations, these steps are:

Solve the equations of motion for the auxiliary fields:

$$(4.17) \quad \frac{\partial F}{\partial \Upsilon_i} = \oint_C \frac{d\zeta}{2\pi i \zeta} \zeta^i \left(\frac{\partial}{\partial \Upsilon} f(\Upsilon, \bar{\Upsilon}; \zeta) \right) = 0, \quad i \geq 2.$$

Solving these equations puts us on $\mathcal{N} = 2$ -shell, which means that only the $\mathcal{N} = (2, 2)$ component symmetry remains off-shell. (In fact, insisting on keeping the $\mathcal{N} = (4, 4)$ constraints (3.9) will put us totally on-shell.) In $\mathcal{N} = (2, 2)$ superspace the resulting model, after eliminating X_i , is given by a Lagrangian $K(\phi, \bar{\phi}, \Sigma, \bar{\Sigma})$.

This is dualized to $\tilde{K}(\phi, \bar{\phi}, \tilde{\phi}, \bar{\tilde{\phi}})$ via a Legendre transform

$$(4.18) \quad \begin{aligned} \tilde{K}(\phi, \bar{\phi}, \tilde{\phi}, \bar{\tilde{\phi}}) &= K(\phi, \bar{\phi}, \Sigma, \bar{\Sigma}) - \tilde{\phi} \Sigma - \bar{\tilde{\phi}} \bar{\Sigma} \\ \tilde{\phi} &= \frac{\partial K}{\partial \Sigma}, \quad \bar{\tilde{\phi}} = \frac{\partial K}{\partial \bar{\Sigma}}. \end{aligned}$$

5. HYPERKÄHLER METRICS ON HERMITEAN SYMMETRIC SPACES

This section contains an introduction to the recent paper [2] where the generalized Legendre transform described in the previous section is used to find metrics on the Hermitean symmetric spaces listed in the following table:

Compact	Non-Compact
$U(n + m)/U(n) \times U(m)$	$U(n, m)/U(n) \times U(m)$
$SO(2n)/U(n); Sp(n)/U(n)$	$SO^*(2n)/U(n); Sp(n, \mathbb{R})/U(n)$
$SO(n + 2)/SO(n) \times SO(2)$	$SO_0(n + 2)/SO(n) \times SO(2)$

The special features of these quotient spaces that allow us to find a hyperkähler metric on their co-tangent bundle is the existence of holomorphic isometries and that we are able to find convenient coset representatives.

A simple example of how the coset representative enters in understanding a quotient is given, e.g., in [18]: In \mathbb{R}^{n+1} the sphere S^n forms a representation of $SO(n + 1)$. The isotropy subgroup at the north pole p_0 of S^n is $SO(n)$. Consider another point p on S^n and let $g_p \in SO(n + 1)$ be an element that maps $p_0 \rightarrow p$. The complete set of elements of $SO(n + 1)$ which map $p_0 \rightarrow p$ is thus of the form $g_p SO(n)$, or in other words $S^n = SO(n + 1)/SO(n)$. A coset representative is a choice of element in $g_p SO(n)$, and that choice can make the transport of properties defined at the north pole to an arbitrary point more or less transparent.

An important step in the generalized Legendre transform is to solve the auxiliary field equation (4.17). As outlined in [6] and further elaborated in [19], for Hermitian symmetric spaces the auxiliary fields may be eliminated exactly. In the present case, we start from a solution at the origin $\phi = 0$,

$$(5.19) \quad \Upsilon^{(0)} = \zeta \Sigma^{(0)} .$$

We then extend this solution to a solution Υ^* at an arbitrary point using a coset representative. We illustrate the method in a simple example due to S. Kuzenko.

Example 3.

The Kähler potential for \mathbb{P}^1 is given by

$$(5.20) \quad K(\phi, \bar{\phi}) = \ln(1 + \phi\bar{\phi}) ,$$

and we denote the metric that follows from this by $g_{\phi, \bar{\phi}}$. Here ϕ is a holomorphic coordinate which we extend to an $\mathcal{N} = (2, 2)$ chiral superfield. To construct a hyperkähler metric we first replace $\phi \rightarrow \Upsilon$, and then solve the auxiliary field equation as in (5.19). Thinking of $\mathbb{C}\mathbb{P}^n$ as the quotient $G_{1, n+1}(\mathbb{C}) = U(n + 1)/U(n) \times U(1)$, we use a coset representative $L(\phi, \bar{\phi})$ to extend the solution from the origin to an arbitrary point. The result is

$$(5.21) \quad \Upsilon^* = \frac{\Upsilon^{(0)} + \phi}{1 - \Upsilon^{(0)}\bar{\phi}} = \frac{\zeta \Sigma^{(0)} + \phi}{1 - \zeta \Sigma^{(0)}\bar{\phi}} .$$

To find the chiral multiplet Σ that parametrizes the tangent bundle, we use the definition

$$(5.22) \quad \Sigma \equiv \frac{d\Upsilon^*}{d\zeta} \Big|_{\zeta=0} = (1 + \phi\bar{\phi})\Sigma^{(0)},$$

yielding

$$(5.23) \quad \Upsilon^* = \frac{(1 + \phi\bar{\phi})\phi + \zeta\Sigma}{(1 + \phi\bar{\phi}) - \zeta\Sigma\bar{\phi}}.$$

The $\mathcal{N} = (2, 2)$ superspace Lagrangian on the tangent bundle is then

$$(5.24) \quad K(\Upsilon^*, \bar{\Upsilon}^*) = K(\phi, \bar{\phi}) + \ln(1 - g_{\phi\bar{\phi}}\Sigma\bar{\Sigma}).$$

The final Legendre transform replacing the linear multiplet by a new chiral field, $\Sigma \rightarrow \tilde{\phi}$ produces the Kähler potential $K(\phi, \bar{\phi}, \tilde{\phi}, \bar{\tilde{\phi}})$ for the Eguchi-Hanson metric.

The \mathbb{P}^1 example captures the essential idea in our construction. The reader is referred to the paper [2] for details.

6. OTHER ALTERNATIVES IN PROJECTIVE SUPERSPACE

Of the two methods for constructing hyperkähler metrics introduced in [22], we have dwelt on the Legendre transform method and its generalization to projective superspace. The hyperkähler reduction (hyperkähler quotient construction) that we further elaborated on in [12], may also be lifted to projective superspace. Both these methods involve only chiral $\mathcal{N} = (2, 2)$ superfields. When a nonzero B -field is present, the $\mathcal{N} = (2, 2)$ sigma models involve all the superfields in (2.5), as discussed in Section 2. For a full description of (generalizations of) hyperkähler metrics on such spaces, the doubly projective superspace [3] is required. We now briefly touch on this construction.

In the doubly projective superspace, at each point in ordinary superspace we introduce one \mathbb{P}^1 for each chirality and denote the corresponding coordinates by ζ_L and ζ_R . The condition (3.7) turns into

$$(6.25) \quad \begin{aligned} \nabla_+(\zeta_L) &= \mathbb{D}_{2+} + \zeta_L\mathbb{D}_{1+}, \\ \nabla_-(\zeta_R) &= \mathbb{D}_{2+} + \zeta_R\mathbb{D}_{1-}, \end{aligned}$$

with the conjugated operators defined with respect to the real structure \mathfrak{A} acting on both ζ_L and ζ_R . A superfield has the expansion

$$(6.26) \quad \Upsilon = \sum_{i,j} \Upsilon_{i,j} \zeta_L^i \zeta_R^j,$$

and is taken to be both left and right projectively chiral. We may also impose reality conditions using \mathfrak{A} , as well as particular conditions on the components, such as the ‘‘cylindrical’’ condition

$$(6.27) \quad \Upsilon_{i,j+k} = \Upsilon_{i,j},$$

for some k . Actions are formed in analogy to (4.15) and (4.16). The $\mathcal{N} = (2, 2)$ components of such a model include twisted chiral fields χ , as well as semi-chiral ones $\mathbb{X}_{L,R}$. In fact this is the context in which the semi-chiral $\mathcal{N} = (2, 2)$ superfields

were introduced [3]. Hyperkähler metrics derived in this superspace are discussed in [20]. An exciting project is to merge this picture with the recent results in [26].

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